

Quantum and classical criticality in a dimerized quantum antiferromagnet

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A quantum critical point (QCP) is a singularity in the phase diagram arising due to quantum mechanical fluctuations. The exotic properties of some of the most enigmatic physical systems, including unconventional metals and superconductors, quantum magnets, and ultracold atomic condensates, have been related to the importance of the critical quantum and thermal fluctuations near such a point. However, direct and continuous control of these fluctuations has been difficult to realize, and complete thermodynamic and spectroscopic information is required to disentangle the effects of quantum and classical physics around a QCP. Here we achieve this control in a high-pressure, high-resolution neutron scattering experiment on the quantum dimer material TiCuCl_3 . By measuring the magnetic excitation spectrum across the entire quantum critical phase diagram, we illustrate the similarities between quantum and thermal melting of magnetic order. We prove the critical nature of the unconventional longitudinal (“Higgs”) mode of the ordered phase by damping it thermally. We demonstrate the development of two types of criticality, quantum and classical, and use their static and dynamic scaling properties to conclude that quantum and thermal fluctuations can behave largely independently near a QCP.

In “classical” isotropic antiferromagnets, the excitations of the ordered phase are gapless spin waves emerging on the spontaneous breaking of a continuous symmetry [1]. The classical phase transition, occurring at the critical temperature T_N , is driven by thermal fluctuations. In quantum antiferromagnets, quantum fluctuations suppress long-range order, and can destroy it completely even at zero temperature [2]. The ordered and disordered phases are separated by a quantum critical point (QCP), where quantum fluctuations restore the broken symmetry and all excitations become gapped, giving them characteristics fundamentally different from the Goldstone modes on the other side of the QCP (Fig. 1). At finite temperatures around a QCP, the combined effects of quantum and thermal fluctuations bring about a regime where the characteristic energy scale of spin excitations is the temperature itself, and this quantum critical (QC) regime has many special properties [3].

Physical systems do not often allow the free tuning of a quantum fluctuation parameter through a QCP. The QC regime has been studied in some detail in heavy-fermion

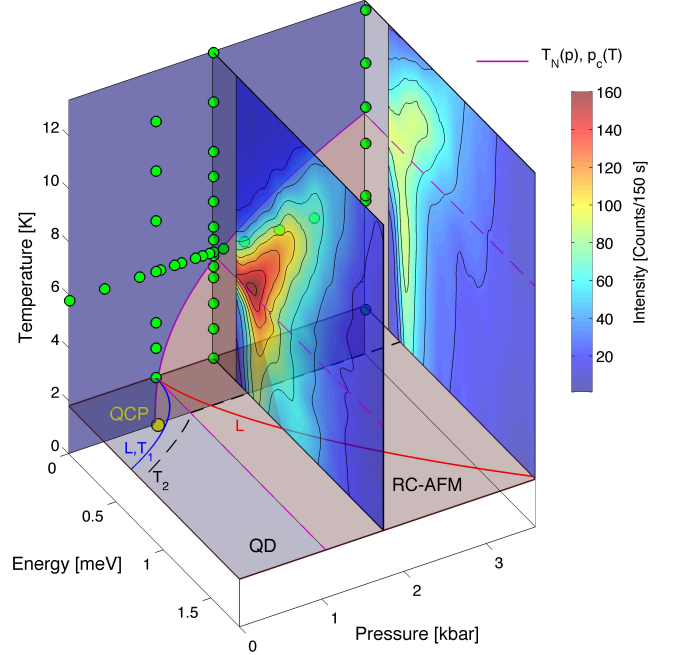


FIG. 1: Pressure-temperature phase diagram of TiCuCl_3 extended to finite energies, revealing quantum and thermal critical dynamics. The rear panel is the bare (p, T) phase diagram at energy $E = 0$ meV, in which the magenta line shows the Néel temperature as a function of pressure, $T_N(p)$ [14], and the green points depict the temperature and pressure values studied. Full details of this panel are presented in Fig. 4(c). The centre (E, T) panel shows neutron intensity data collected from $T = 1.8$ K to 12.7 K at $p = 1.75$ kbar, where $T_N = 5.8$ K. The rightmost (E, T) panel shows the corresponding data at $p = 3.6$ kbar, where $T_N = 9.2$ K. The data in both (E, T) panels display a clear softening of the magnetic excitations at $T_N(p)$. The bottom (p, E) panel indicates the softening of the excitations, measured at $T = 1.8$ K, across the QPT [19]. T_1 , T_2 and L denote the three gapped triplet excitations of the quantum disordered (QD) phase. In the renormalized classical antiferromagnetic (RC-AFM) ordered phase, these become respectively the gapless Goldstone mode, which is a transverse spin wave, a gapped (anisotropic) spin wave, and the longitudinal “Higgs” mode (see text).

metals with different dopings, where the quantum phase transition (QPT) is from itinerant magnetic phases to unusual metallic or superconducting ones [4–6], in organic materials where a host of insulating magnetic phases become (super)conducting [7, 8], and in cold atomic gases tuned from superfluid to Mott-insulating states [9, 10]. However, the dimerized quantum spin system TiCuCl_3 occupies a very special position in the experimental study

of QPTs. The quantum disordered phase at ambient pressure and zero field has a small gap to spin excitations. An applied magnetic field closes this gap, driving a QPT to an ordered phase, a magnon condensate in the Bose-Einstein universality class, with a single, nearly massless excitation [11, 12].

Far more remarkably, an applied pressure also drives a QPT to an ordered phase [13], occurring at the very low critical pressure $p_c = 1.07$ kbar [14] and sparking detailed studies [15, 16]. This ordered phase is a different type of condensate, whose defining feature is a massive excitation, a “Higgs boson” or longitudinal fluctuation mode of the weakly ordered moment [17, 18]. This excitation, which exists alongside the two transverse (Goldstone) modes of a conventional well-ordered magnet, has been characterized in detail by neutron spectroscopy with continuous pressure control through the QPT [19] and subsequently by different theoretical approaches [20, 21]. TiCuCl_3 is therefore an excellent system for answering fundamental questions about the development of criticality, the nature of the QC regime, and the interplay of quantum and thermal fluctuations by controlling both the pressure and the temperature.

Here we present inelastic neutron scattering (INS) results which map the evolution of the spin dynamics of TiCuCl_3 throughout the quantum critical phase diagram in pressure and temperature. The spin excitations we measure exhibit different forms of dynamical scaling behaviour arising from the combined effects of quantum and thermal fluctuations, particularly on crossing the QC regime and at the line of phase transitions to magnetic order (Fig. 1). To probe these regions, we collected spectra up to 1.8 meV for temperatures between $T = 1.8$ K and 12.7 K, and over a range of pressures. Our measurements were performed primarily at $p = 1.05$ kbar ($\simeq p_c$ at the lowest temperatures), 1.75 kbar, and 3.6 kbar, and also for all pressures at $T = 5.8$ K. Most measurements were made at the ordering wavevector, $\mathbf{Q}_0 = (0\ 4\ 0)$ reciprocal lattice units (r.l.u.), and so concern triplet mode gaps. From the INS selection rules, only one transverse mode of the ordered phase is observable at $\mathbf{Q} = \mathbf{Q}_0$, and it is gapped ($\Delta_a = 0.38$ meV) due to a 1% exchange anisotropy [19]. In the summary presented in Fig. 1, the contours represent scattered intensities at two selected pressures $p > p_c$. Both panels show strong QC scattering and a nontrivial evolution of the mode gaps and spectral weights with both p and T , which is quantified in Fig. 2.

Figures 2(a-c) show respectively the measured intensities for pressures below, at, and above the QPT at a fixed low temperature. Fits to the lineshapes of the separate excitations were made by a resolution deconvolution requiring both the gap and the local curvature of the mode dispersion, which was taken from a finite-temperature bond-operator description [22, 23]. The distinct contributions from transverse and longitudinal fluctuations change position systematically as the applied pressure induces magnetic order. The intensity of the longitudinal mode is highlighted in red in Fig. 2(c). Figures 2(d-f) show respectively the measured intensities for temperatures below, at, and above the phase transition [$T_N(p)$]

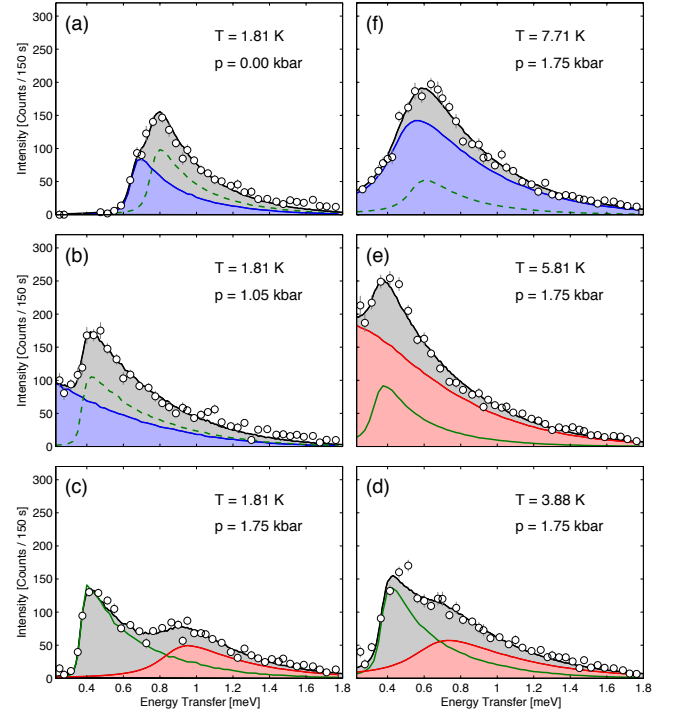


FIG. 2: INS spectra collected at $\mathbf{Q} = (0\ 4\ 0)$ r.l.u., the wavevector of the minimum energy gap in the QD phase, where magnetic order is induced with increasing pressure. (a-c) Evolution of triplet excitations during pressure-induced magnetic ordering, as the lower mode (L and T_1 , blue) changes continuously into the longitudinal mode (L, red), while the anisotropic mode (T_2 , green) remains gapped. (d-f) Evolution as increasing temperature lowers the longitudinal-mode gap to zero at $T = 5.8$ K, above which all three modes are gapped in a disordered (QC) state.

at a fixed pressure $p > p_c$. Quantitatively, the intensity and the linewidth increase from the left to the right panels due to the temperature. Qualitatively, the thermal evolution is almost exactly analogous to a change in the pressure, with the spectral weight of the longitudinal mode softening at $T_N(p = 1.75 \text{ kbar}) = 5.8$ K but moving again to finite energies at temperatures above T_N .

We analyze these results in detail by extracting the excitation energies $\epsilon_{\mathbf{Q}}$ and linewidths $\Gamma_{\mathbf{Q}}$ from the data of Fig. 2. Figure 3(a) shows the evolution of the mode gaps ($\epsilon_{\mathbf{Q}=\mathbf{Q}_0}$) with pressure for $T = 1.8$ K (the QPT, *cf.* Ref. [19]) and $T = 5.8$ K. The longitudinal mode of the ordered phase appears on the right, and softens with decreasing pressure until $p_c(T)$. The Goldstone mode is not visible due to the scattering geometry. At pressures below $p_c(T)$, the effect of dimer-based quantum fluctuations is to destroy the magnetic order and gap all the modes. The lines are best fits to power laws of the form $\Delta(p) = A|p - p_c|^{\gamma_p}$, which we discuss below.

Figure 3(b) shows the evolution of the mode gaps over the temperature range $1.8 \text{ K} < T < 12.7 \text{ K}$ for pressures $p = 1.75$ kbar and 3.6 kbar. Here the ordered phase is on the left, where the longitudinal mode, which dominates the low-energy scattering around the critical point, becomes soft at a Néel temperature $T_N(p)$ determined by the pressure. They reemerge on the right as gapped triplets of the thermally disordered QC phase.

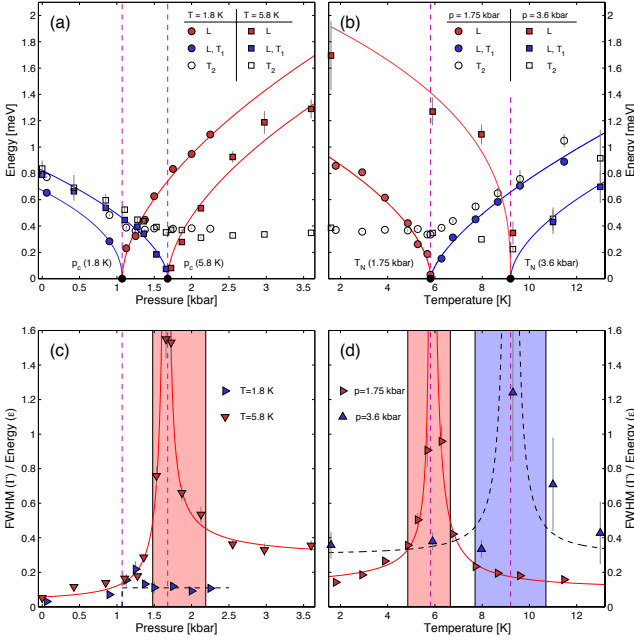


FIG. 3: Spin dynamics at the quantum and thermal “melting” transitions. (a) Quantum melting of magnetic order, shown by the triplet gaps for two different temperatures ($T = 1.8$ and 5.8 K), occurs from right to left. (b) Thermal melting, shown for two different pressures ($p = 1.75$ kbar and 3.6 kbar), occurs from left to right. Open black circles and squares give the energies of the anisotropic transverse excitations (T_2), which remain gapped, while filled circles and open squares show the longitudinal mode (red in the ordered phase, blue in the disordered one). The lines are power-law fits, described in the text. (c,d) Linewidth-to-energy ratios Γ_Q/ϵ_Q for the longitudinal mode across the phase transition as a function of pressure at $T = 1.8$ and 5.8 K (c) and of temperature at $p = 1.75$ and 3.6 kbar (d); lines are guides to the eye and shaded regions are explained in the text.

The lines in this figure are best fits to power laws of the form $\Delta(T) = B|T - T_N|^{\gamma_T}$. The similarity between quantum and thermal melting shown in Figs. 2 and 3 is a remarkable result. It is essential to note that the disorder in Fig. 3(b) is thermal, and not due to quantum fluctuations. Thermal fluctuations in a quantum dimer system, whose triplet excitations are hard-core bosons, do not simply broaden and damp the modes of the ordered magnet, but cause a very specific and systematic evolution of the spectral weight [22]. On the ordered side, the massive, longitudinal mode becomes gapless at the classical phase transition, while on the disordered side there is not merely a featureless paramagnet but a clear gapped excitation. This is also the case for the pressure-driven transition at finite temperatures [Fig. 3(a)], where the symmetry is restored before all three excitations become gapped modes of the QC phase.

Figures 3(c) and (d) show the linewidths of the longitudinal mode, measured respectively through the quantum and thermal transitions, in the form of the ratio $\Gamma_Q/\epsilon_Q = \alpha_L$. For the pressure-induced phase transition in Fig. 3(c), the ratio vanishes at $T = 1.8$ K for the well-defined excitations on the disordered side and remains constant (with $\alpha_L \simeq 0.15$) on the ordered side of the QCP, demonstrating its critically damped nature

[19]. However, this is not at all the case at $T = 5.8$ K, where the divergence of $\alpha_L(T)$ shows the longitudinal mode becoming overdamped in the presence of thermal fluctuations. For the thermally driven phase transition at $p = 1.75$ and 3.6 kbar [Fig. 3(d)], the ratio also diverges on approaching the critical temperature $T_N(p)$.

The QC regime is the area around the line $p = p_c$ where the intrinsic energy scale of the system (the gap Δ in the QD phase, or T_N in the ordered phase [2]) is lower than the temperature [3]. Near p_c , the measured neutron intensities [Fig. 4(a)] show a broad range over which spin excitations are present, with a peak along a line corresponding approximately to $\hbar\epsilon_Q = k_B T$. This “ ω/T ” scaling property [3] is evident in the self-similar nature of the spectra at different temperatures. The QCP is the point where the intrinsic energy scale vanishes, and thus states become available at all energies; it is the maximum in their occupation that scales with T , and hence the temperature becomes the new characteristic energy scale. The microscopic origin of this “thermal gap” in the measured spectrum is mutual blocking of the hard-core triplet excitations [22]. As shown in Fig. 4(b), the linewidth $\Gamma_Q = \alpha_c \epsilon_Q$ ($\alpha_c \simeq 0.14$) also scales linearly with T , illustrating that critical damping is an essential property of QC excitations.

The experimental phase diagram is shown in Fig. 4(c), and contains all four regions characteristic of the QCP [3, 4]. Between the quantum disordered and renormalized classically ordered regimes [2], the dominant behaviour is QC (ω/T) scaling. On the line of classical phase transitions, the intrinsic energy scale is $T_N(p)$ but the excitation energy is driven to zero. This results in the properties, in particular the static scaling relations, of a classical critical (CC) regime. We show below that the scaling exponents in the QC and CC regions have approximately the values expected theoretically. However, for a real system such as TiCuCl_3 , they can differ over broad crossover regions determined by the relative size of the intrinsic and excitation energy scales, and departures from universal behaviour may also arise due to microscopic details of the Hamiltonian.

We begin the analysis of our results not with static exponents but with the dynamical ones extracted from the power-law fits to the gaps in Figs. 3(a) and (b). At the pressure-controlled transition, all of the exponents we measure fall in the range $0.46(6) \leq \gamma_p \leq 0.57(6)$, which within experimental error is $\gamma_p = 1/2$. This is the mean-field expectation in the generic case that the p -dependence of the exchange parameters $J_{ij}(p)$ is predominantly linear [19]. It applies both for the disordered phase (Δ_{QD}) and for the gap (Δ_L) of the longitudinal mode, with a multiplicative prefactor $\Delta_L = \sqrt{2}\Delta_{QD}$ at $T = 0$ [25]. At higher temperatures we find no strong departures from universality in this exponent. However, fits including data points at the higher energies are generally less reliable, suggesting that these begin to depart from the universal regime.

For the classical (temperature-controlled) phase transition, the expectation for the QC phase is $\Delta \propto \xi^{-1} \propto (T - T_N)^{\nu}$, where $\nu \simeq 0.67$ for an XY spin symmetry and 0.70 for SU(2) symmetry [26]. The 1% exchange

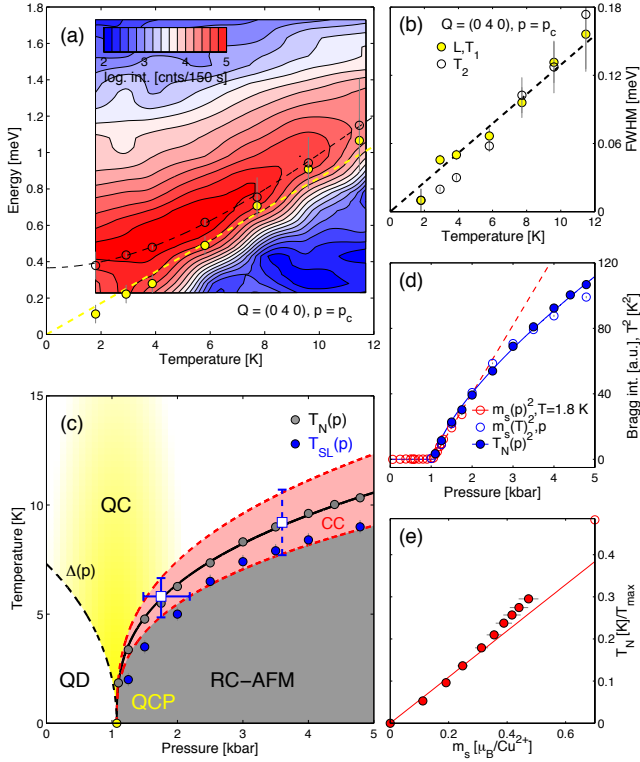


FIG. 4: Quantum and classical criticality. (a) Scattered neutron intensity at $p = p_c$ as a function of temperature. Points show the energies $\epsilon_{\mathbf{Q}}$ extracted from the intensity for the modes becoming gapless (L and T_1 , yellow) and gapped (T_2 , black) as $T \rightarrow 0$. (b) $\Gamma_{\mathbf{Q}}$ as a function of T at $p = p_c$. (c) Complete experimental phase diagram, showing quantum disordered (QD), quantum critical (QC), classical critical (CC), and renormalized classical (RC-AFM) phases. The dashed lines denote energy scales marking crossovers in behaviour. Grey symbols denote $T_N(p)$ [14], blue symbols labelled $T_{SL}(p)$ show the limit of classical critical scaling in the data for the staggered magnetization, $m_s(T)$, and the blue bars are taken from $\Gamma_{\mathbf{Q}}/\epsilon_{\mathbf{Q}}(T)$ (see text). (d) Linear proportionality of the measured $T_N(p)$ and $m_s(p)$ [14]. (e) Scaling of T_N and m_s , including one high- p data point taken from Ref. [24] for an absolute calibration of the ordered moment. Red lines in panels (d) and (e) represent scaling behaviour discussed in the text.

anisotropy in TiCuCl_3 reduces the spin symmetry from $\text{SU}(2)$ to XY below energy scales of order 5 K. Our data for γ_T at $p = 1.75$ kbar give $\gamma_T = 0.67(9)$, in excellent agreement with these exponents; at $p = 3.6$ kbar we do not have sufficient data for a reliable fit. At $p = p_c$, however, we find the expected QC scaling form $\gamma_T = 1$, and the width of the crossover regime remains an open question. Deducing a scaling exponent γ_T for the T -dependence of the longitudinal mode gap in the ordered phase remains a current theoretical challenge. For this it is important to recall that at finite temperature this Higgs mode becomes weakly overdamped, and what we show is the associated maximum in scattering intensity. For $p = 1.75$ kbar we find $\gamma_T = 0.54(8)$.

Further insight into thermal scaling exponents can be obtained from the staggered magnetic moment, m_s , measured in Ref. [14]. Fits to the form $m_s \propto (T_N - T)^{\beta'}$ yield values close to the classical field-theory expectation [26] $\beta' = 0.34$ (XY) or 0.37 [SU(2)]. However, the fit is

followed only in a narrow window $T_{SL}(p) < T \leq T_N(p)$, with $T_{SL} \simeq 0.8T_N$ and points further away from the transition diverging clearly from classical scaling [14]. Thus m_s represents very well the scaling relations expected for a narrow CC regime in a system dominated by a QCP [Fig. 4(c)]. The narrow nature of the CC region is also evident in dynamical properties, in that the divergence of the QC and longitudinal mode widths may be used to set dynamical criteria for the crossover from QC to CC scaling. On the right side of Figs. 3(c), α_L approaches a constant also at finite T , but diverges on approaching $p_c(T)$ (on the left side $\alpha \rightarrow 0$ towards the QD regime). In Fig. 3(d), quantum behaviour is evident in the constant values of α reached far from the critical points, a regime including the QC excitations around the line $p = p_c$ (where $\alpha = \alpha_c$). We define classical scaling when $\alpha > 1/2$, giving the shaded regions shown in Figs. 3(c) and (d). The largely symmetric form of the $\Gamma_{\mathbf{Q}}/\epsilon_{\mathbf{Q}}$ curves is the best available indicator for a classical scaling regime on the disordered side of $T_N(p)$. These parallel static and dynamic approaches indicate the width of the CC regime in both pressure and temperature [Fig. 4(c)].

Our precise level of control over quantum criticality in TiCuCl_3 has inspired recent numerical and analytical studies of the finite- T properties of dimer systems at the coupling-induced QPT. The authors of Ref. [16] argue that $m_s(p)$ and $T_N(p)$ should have the same behaviour, and demonstrate good scaling of m_s with T_N by Quantum Monte Carlo simulations, independent of the functional form in p ; this technique cannot address the longitudinal mode. In an effective quantum field theory approach [20], $m_s(p) \propto T_N(p) \propto \sqrt{p - p_c}$ for a linear p -dependence of the exchange couplings, and $\Delta_L(p)$ also has this dependence. This analysis is predicated on proximity to a QCP, but in neglecting the classical critical regime, the field theory does not return the correct behaviour for static quantities around T_N , although its dynamical predictions remain valid. The exchange anisotropy in TiCuCl_3 is found [20] to have small quantitative effects on the calculated quantities, but no detectable qualitative ones (*e.g.* on exponents). From our measurements, the best fits to the pressure exponents for m_s and T_N lie close to the classical value of 0.35 [14], although the quantum value of 0.5 is not beyond the error bars very close to the QCP. From experiment, the two quantities scale well together near the QCP, as shown in Figs. 4(d) and (e), but depart from universal scaling [16] around an ordered moment of $0.4\mu_B/\text{Cu}$ [Fig. 4(e)].

We have shown that the effects on the spectrum of quantum and thermal melting are qualitatively very similar. Both result in the systematic evolution of excitations whose gap increases away from the classical phase transition line, rather than simply a loss of coherence due to thermal fluctuations. Microscopically, quantum fluctuations in a dimer-based system cause enhanced singlet formation and loss of interdimer magnetic correlations, while thermal fluctuations act to suppress the spin correlation function $\langle \mathbf{S}_i \cdot \mathbf{S}_j \rangle$ on both the dimer and interdimer bonds. These correlation functions may be estimated from neutron-scattering intensities [23] and also measured in dimerized optical lattices of ultracold fermions

[28]. In TiCuCl_3 , both methods of destroying interdimer coherence cause the triplet modes to evolve in the same way. A key question in the understanding of quantum criticality is whether quantum and thermal fluctuations can be considered as truly independent, and whether this independence may be taken as a definition of the QC regime [16]. Our experimental results suggest that weak departures from universality become detectable at (p, T) values away from the QC and CC regimes, and particularly as we increase the excitation energy, presumably as microscopic details of the fluctuation redistribution cause a mixing of quantum and thermal effects.

Finally, the existence of the longitudinal “Higgs” mode has been questioned in the past. Its visibility has recently been analyzed in detail in the scaling limit [21, 27] for systems in two and three dimensions. Our results confirm that it is a genuine example of quantum critical dynamics in three dimensions. Its critical nature makes it infinitely susceptible to thermal fluctuations, so that it becomes overdamped as soon as these become noticeable. While still possessing a significant spectral weight, the longitudinal mode of the pressure-ordered phase is overdamped at finite temperatures, although its critical nature is restored on passing into the finite- T disordered phase. There are several reasons for the ready visibility – in the longitudinal rather than the scalar susceptibility [21] – of the longitudinal mode in TiCuCl_3 , meaning for the anomalously low value of α_L , despite its critically damped nature. These include the high dimensionality of the system, its low phase space for magnon scattering, the collinearity of the ordered moments, and the fact that one of the spin waves contributing to decay processes is massive. It is reasonable to assume that the same factors also control the anomalously low value of α_c , allowing ready observation of the QC excitations at $p = p_c$ [Figs. 4(a) and (b)], and the very narrow regime of logarithmic corrections to scaling [29], which are completely absent in our data. Both the visibility of the longitudinal mode and our level of control over both quantum and thermal fluctuations in TiCuCl_3 remain significantly superior to any other magnetic [17, 18], charge-density-wave [31], or cold-atom [32] systems displaying this “Higgs boson.”

In summary, high-resolution neutron spectroscopy experiments on the quantum antiferromagnet TiCuCl_3 allow us to probe the spin excitations of all phases in and around the QC regime by varying the pressure and temperature. We demonstrate a number of remarkable properties arising at the interface between quantum and classical physics. Quantum and thermal fluctuations have remarkably similar effects in melting the magnetically ordered phase and in opening excitation gaps, but operate quite independently close to the QCP. In the QC regime there is robust ω/T scaling of the energies and widths of critically damped excitations. This scaling crosses over to a classical critical form in a narrow region around the phase transition line $T_N(p)$. The critically damped longitudinal, or Higgs, mode of the ordered phase is exquisitely sensitive to thermal fluctuations and becomes overdamped in the classical regime.

Materials and Methods

High-quality single crystals of TiCuCl_3 were grown by the Bridgman method. INS studies were performed on the cold-neutron triple-axis spectrometer IN14 at the Institut Laue Langevin (ILL). This was operated at constant final wavevector $k_f = 1.15 \text{ \AA}^{-1}$, with a focusing pyrolytic graphite analyser and monochromator, collimation open-60°-open-open and a cooled Be filter positioned between sample and analyser. The temperature and pressure were controlled with a He cryostat and a He gas pressure cell (precision ± 50 bar). We fitted our experimental measurements with a thermal damping ansatz [33], which has been used for the accurate modelling of phonon damping at finite temperatures [34] and shown in Ref. [22] to be reliable for triplet spin excitations. The magnon is modelled as a damped harmonic oscillator (DHO), whose scattering intensity has the double-Lorentzian lineshape

$$S(\mathbf{Q}, \omega) = \frac{A[n(\omega) + 1]4\Gamma_{\mathbf{Q}}\epsilon_{\mathbf{Q}}\omega}{[\omega^2 - \epsilon_{\text{DHO}}(\mathbf{Q})^2]^2 + 4\Gamma_{\mathbf{Q}}^2\omega^2}, \quad (1)$$

where $n(\omega)$ expresses the thermal magnon population. Here $\epsilon_{\text{DHO}}(\mathbf{Q})^2 = \epsilon_{\mathbf{Q}}^2 + \Gamma_{\mathbf{Q}}^2$ is a renormalized energy expressed in terms of the real excitation energy, $\epsilon_{\mathbf{Q}}$, and the linewidth of the scattered intensity, taken as the FWHM, $\Gamma_{\mathbf{Q}}$. The fits presented in Fig. 2 are based on a four-dimensional convolution in momentum and energy of the model cross-section [Eq. (1)] with the instrument resolution, which causes the asymmetric peak shapes. Excitations measured throughout the (p, T) phase diagram were characterized in this way by their energies $\epsilon_{\mathbf{Q}}$, linewidths $\Gamma_{\mathbf{Q}}$, and intensities [Eq. (1)].

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Because our data provide no signs of such corrections in either the thermal or the pressure exponents, we conclude that this regime is unusually small in TiCuCl_3 .

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Author contributions

P.M. and Ch.R. carried out the experiments with the help of instrument scientist M.B. TiCuCl_3 single crystals were synthesized by K.W.K. The theoretical and experimental framework was conceived by Ch.R., D.F.M. and B.N. Data refinement and figure preparation were performed by P.M. and Ch.R. The text was written by B.N. and Ch.R.

Additional information

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Competing Financial Interests

The authors declare no competing financial interests.